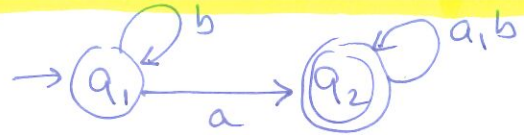


Sei  $\mathcal{A}$ :   $\mathcal{A} = (K, \Sigma, \delta, q_1)$   
 $K = \{q_1, q_2\}, \Sigma = \{a, b\}$

Konstruktion aus dem Hauptsatz von Kleene  
 zur Berechnung eines regulären Ausdruckes  $r$   
 mit  $\mathcal{J}(r) = \mathcal{L}(\mathcal{A})$ .

•  $L(\mathcal{A}) = \bigcup_{q_i \neq q_j} R_{ij}^n = \underline{R_{12}^2}$

wobei 
$$R_{ij}^0 = \begin{cases} \{d \in \{a, b\} \mid \delta(q_i, d) = q_j\} & \text{falls } i \neq j \\ \{d \in \{a, b\} \mid \delta(q_i, d) = q_j\} \cup \{\epsilon\} & \text{falls } i = j \end{cases}$$

$$R_{ij}^{k+1} = R_{ij}^k \cup R_{i, k+1}^k (R_{k+1, k+1}^k)^* R_{k+1, j}^k$$

$R_{ij}^k$	Menge	Reg. Ausdruck
$R_{11}^0$	$\{b\} \cup \{\epsilon\} = \{b, \epsilon\}$	$b + 1$
$R_{12}^0$	$\{a\}$	$a$
$R_{21}^0$	$\emptyset$	$0$
$R_{22}^0$	$\{a, b\} \cup \{\epsilon\} = \{a, b, \epsilon\}$	$a + b + 1$

$$R_{ij}^1 = R_{ij}^0 \cup R_{i1}^0 (R_{11}^0)^* R_{1j}^0$$

$R_{11}^1$	$\{b, \epsilon\} \cup \{b, \epsilon\} \{b, \epsilon\}^* \{b, \epsilon\}$	$b + 1 + (b + 1)(b + 1)^*(b + 1) = b^*$
$R_{12}^1$	$\{a\} \cup \{b, \epsilon\} \{b, \epsilon\}^* \{a\}$	$a + (b + 1)(b + 1)^* a = b^* a$
$R_{21}^1$	$\emptyset \cup \emptyset \{b, \epsilon\}^* \{b, \epsilon\}$	$0 + 0 \cdot (b + 1)^*(b + 1) = 0$
$R_{22}^1$	$\{a, b, \epsilon\} \cup \emptyset \{b, \epsilon\}^* \{a\}$	$a + b + 1$

$$R_{ij}^2 = R_{ij}^1 \cup R_{i2}^1 (R_{22}^1)^* R_{2j}^1$$

$$\underline{R_{12}^2} = R_{12}^1 \cup R_{12}^1 (R_{22}^1)^* R_{22}^1$$

Reg. Ausdruck:  $b^* a + b^* a (a + b + 1)^* (a + b + 1)$   
 $= \underline{b^* a (a + b)^*}$