Universität Koblenz-Landau

FB 4 Informatik

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Exercises for "Formal Specification and Verification" Exercise sheet 4

Exercise 4.1:

You may recall the puzzle of a ferryman, goat, cabbage, and wolf all on one side of a river. The ferryman can cross the river with at most one passenger in his boat. There is a behavioural conflict between:

- 1. the goat and the cabbage; and
- 2. the goat and the wolf;

if they are on the same river bank but the ferryman is not on that river bank (the goat eats the cabbage, resp. the wolf eats the goat).

Define a "program graph" describing this system: (Loc, Act, Effect, \rightarrow , Loc₀) where:

- Loc = { left, right, conflict } is a set of locations with initial locations Loc₀ = { left }. Intuitively, left and right represent the location of the ferryman; conflict represents the conflict situation when the cabbage or the goat is eaten.
- Act = { carry-lr-goat, carry-rl-goat, carry-lr-cabbage, carry-rl-cabbage, carry-lr-wolf, carry-rl-wolf, cross-rl, cross-lr, eat-cabbage, eat-goat } is a set of actions.

(For instance:

- carry-lr-goat means: the ferryman carries the goat from the left to the right river
- carry-rl-goat means: the ferryman carries the goat from the right to the left river bank
- cross-rl (resp. cross-lr) means: the ferryman crosses the river from right to left (left to right) without carrying anything.
- eat-cabbage means: the goat eats the cabbage
 eat-goat means: the wolf eats the goat.)

Assume that $Var = \{goat, cabbage, wolf\}$ and the corresponding domains are $\{l, r\}$.

Let
$$Eval(Var) = \{\beta \mid \beta : Var \rightarrow \{l, r\}\}.$$

(Intuitively, $\beta(x) = l$ means that x is on the left side of the river, and $\beta(x) = r$ means that x is on the right side of the river.)

Assume that $Cond(Var) = \{ \text{goat} \approx l, \text{goat} \approx r, \text{cabbage} \approx l, \text{cabbage} \approx r, \text{wolf} \approx l, \text{wolf} \approx r \}$ and that the initial condition is

$$g_0 := (\mathsf{goat} \approx l) \land (\mathsf{cabbage} \approx l) \land (\mathsf{wolf} \approx l)$$

- (1) Define a suitable effect function Effect: Act × Eval(Var) → Eval(Var).
 (It is not necessary to exhaustively present the definition of this function, you can present some examples and explain how it is defined in general)
- (2) Define a suitable transition relation $\to \subseteq \mathsf{Loc} \times (Cond(\mathsf{Var}) \times \mathsf{Act}) \times \mathsf{Loc}$ such that there is no $\phi \in Cond(\mathsf{Var}), \alpha \in Act, l \in \mathsf{Loc}$ such that (conflict, ϕ, α, l) $\in \to$.

 (It is not necessary to exhaustively present the definition of the transition relation \to ; you can explain how it is defined in general and give some examples)
- (3) Describe the transition system TS(PG) = (S, Act, →, I, AP, L) of the program graph (Loc, Act, Effect, →, Loc₀, g₀) constructed before.
 (It is not necessary to exhaustively present the definition of the transition relation → or the labelling function; you can explain how they are defined in general and give some examples)
- (4) Describe:
 - Post(<left, $\beta >$, carry-lr-goat), where $\beta(\mathsf{goat}) = l$, $\beta(\mathsf{cabbage}) = \beta(\mathsf{wolf}) = r$.
 - Post($\langle \text{left}, \beta \rangle$, carry-rl-goat), where $\beta(\text{goat}) = l, \beta(\text{cabbage}) = \beta(\text{wolf}) = r$.
 - Post($\langle \text{left}, \beta \rangle$), where $\beta(\text{goat}) = l, \beta(\text{cabbage}) = \beta(\text{wolf}) = r$.
 - Post(<right, $\beta >$), where $\beta(goat) = \beta(cabbage) = l, \beta(wolf) = r$.
 - Post({<right, β >,<right, β' >}), where $\beta(\text{goat}) = \beta(\text{cabbage}) = l, \beta(\text{wolf}) = r$ and $\beta'(\text{goat}) = \beta(\text{wolf}) = l, \beta(\text{cabbage}) = r$
 - Pre(<conflict, $\beta >$), where β (goat) = β (cabbage) = l, β (wolf) = r.
 - Pre(<conflict, $\beta >$), where β (goat) = β (wolf) = β (cabbage) = r.
- (5) Is the transition system you constructed action-deterministic? Is it AP-deterministic?
- (7) Are there terminal states in the system?
- (8) Is the state $\langle \text{right}, \beta \rangle$ with $\beta(\text{goat}) = \beta(\text{cabbage}) = \beta(\text{wolf}) = r$ reachable?

Please submit your solution until Wednesday, June 4, 2014 at 11:00. Please do not forget to write your name on your solution.

Submission possibilities:

- By e-mail to sofronie@uni-koblenz.de with the keyword "Homework FSV" in the subject.
- Hand it in to me (Room B225) or drop it in the box in front of Room B224.