## Universität Koblenz-Landau **FB 4 Informatik**

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## Exercises for "Formal Specification and Verification" Exercise sheet 4

## Exercise 4.1:

You may recall the puzzle of a ferryman, goat, cabbage, and wolf all on one side of a river. The ferryman can cross the river with at most one passenger in his boat. There is a behavioural conflict between:

- 1. the goat and the cabbage; and
- 2. the goat and the wolf;

if they are on the same river bank but the ferryman is not on that river bank (the goat eats the cabbage, resp. the wolf eats the goat).

Define a "program graph" describing this system:  $(Loc, Act, Effect, \rightarrow, Loc_0)$  where:

- $Loc = \{ left, right, conflict \}$  is a set of locations with initial locations  $Loc_0 = \{ left \}$ . Intuitively, left and right represent the location of the ferryman; conflict represents the conflict situation when the cabbage or the goat is eaten.
- Act = { carry-lr-goat, carry-rl-goat, carry-lr-cabbage, carry-rl-cabbage, carry-lr-wolf, carry-rl-wolf, cross-rl, cross-lr, eat-cabbage, eat-goat } is a set of actions.

(For instance:

- carry-lr-goat means: the ferryman carries the goat from the left to the right river bank
- carry-rl-goat means: the ferryman carries the goat from the right to the left river bank
- cross-rl (resp. cross-lr) means: the ferryman crosses the river from right to left (left to right) without carrying anything.
- eat-cabbage means: the goat eats the cabbage
  eat-goat means: the wolf eats the goat.)

Assume that  $Var = \{goat, cabbage, wolf\}$  and the corresponding domains are  $\{l, r\}$ . Let  $\text{Eval}(\text{Var}) = \{\beta \mid \beta : \text{Var} \rightarrow \{l, r\}\}.$ 

(Intuitively,  $\beta(x) = l$  means that x is on the left side of the river, and  $\beta(x) = r$  means that x is on the right side of the river.)

Assume that  $Cond(Var) = \{ goat \approx l, goat \approx r, cabbage \approx l, cabbage \approx r, wolf \approx l, wolf \approx r \}$ and that the initial condition is

$$g_0 := (\text{goat} \approx l) \land (\text{cabbage} \approx l) \land (\text{wolf} \approx l)$$

(1) Define a suitable effect function  $\mathsf{Effect} : \mathsf{Act} \times \mathsf{Eval}(\mathsf{Var}) \to \mathsf{Eval}(\mathsf{Var})$ .

(It is not necessary to exhaustively present the definition of this function, you can present some examples and explain how it is defined in general)

- (2) Define a suitable transition relation → ⊆ Loc × (Cond(Var) × Act) × Loc such that there is no φ ∈ Cond(Var), α ∈ Act, l ∈ Loc such that (conflict, φ, α, l) ∈→.
  (It is not necessary to exhaustively present the definition of the transition relation →; you can explain how it is defined in general and give some examples)
- (3) Describe the transition system  $TS(PG) = (S, Act, \rightarrow, I, AP, L)$  of the program graph (Loc, Act, Effect,  $\rightarrow$ , Loc<sub>0</sub>,  $g_0$ ) constructed before.

(It is not necessary to exhaustively present the definition of the transition relation  $\rightarrow$  or the labelling function; you can explain how they are defined in general and give some examples)

- (4) Describe:
  - Post(<left,  $\beta$  >, carry-lr-goat), where  $\beta$ (goat) =  $l, \beta$ (cabbage) =  $\beta$ (wolf) = r.
  - Post(<left,  $\beta$  >, carry-rl-goat), where  $\beta$ (goat) =  $l, \beta$ (cabbage) =  $\beta$ (wolf) = r.
  - Post(<left,  $\beta$  >), where  $\beta$ (goat) =  $l, \beta$ (cabbage) =  $\beta$ (wolf) = r.
  - Post(<right,  $\beta >$ ), where  $\beta$ (goat) =  $\beta$ (cabbage) =  $l, \beta$ (wolf) = r.
  - Post({<right,  $\beta >$ , <right,  $\beta' >$ }), where  $\beta(\text{goat}) = \beta(\text{cabbage}) = l, \beta(\text{wolf}) = r$ and  $\beta'(\text{goat}) = \beta(\text{wolf}) = l, \beta(\text{cabbage}) = r$
  - $Pre(\langle conflict, \beta \rangle)$ , where  $\beta(goat) = \beta(cabbage) = l$ ,  $\beta(wolf) = r$ .
  - $Pre(\langle conflict, \beta \rangle)$ , where  $\beta(goat) = \beta(wolf) = \beta(cabbage) = r$ .
- (5) Is the transition system you constructed action-deterministic? Is it AP-deterministic?
- (7) Are there terminal states in the system?
- (8) Is the state  $\langle \text{right}, \beta \rangle$  with  $\beta(\text{goat}) = \beta(\text{cabbage}) = \beta(\text{wolf}) = r$  reachable?

Please submit your solution until Wednesday, December 14, 2016 at 12:00. Please do not forget to write your name on your solution.

Submission possibilities:

- By e-mail to sofronie@uni-koblenz.de with the keyword "Homework FSV" in the subject.
- Hand it in to me (Room B225) or drop it in the box in front of Room B224.