

Beispiel 1

$$\Sigma = (\Sigma, \pi) \quad \Sigma = \{a/0, f/1\}$$

$$T_\Sigma = \{a, f(a), f(f(a)), \dots, f(f(\dots f(a))) \dots\}$$

$$= \{f^n(a) \mid n \in \mathbb{N}\}$$

$$A = (U_A, \{f_A : U_A \rightarrow U_A ; a_A \in U_A\}, \dots)$$

$$A = (T_\Sigma, \{f_A : T_\Sigma \rightarrow T_\Sigma, a_A \in T_\Sigma\}, \dots)$$

$$a_A = a \in T_\Sigma$$

$$f_A : T_\Sigma \rightarrow T_\Sigma$$

$$f_A(f^n(a)) = f(f^n(a)) = f^{n+1}(a)$$

$$\text{z.B.: } f_A(a) = f(a)$$

$$f_A(f(a)) = f(f(a))$$

$$f_A(f(f(a))) = f(f(f(a)))$$

Beispiel 2

$$\Sigma = (\Sigma, \pi) \quad \Sigma = \{a/0, b/0, c/0\}$$

$$T_\Sigma = \{a, b, c\}$$

$$A = (\{a, b, c\}, \{a_A, b_A, c_A \in \{a, b, c\}\}, \dots)$$

$$a_A = a$$

$$b_A = b$$

$$c_A = c$$

Beispiel 3

$$\Sigma = (\Sigma, \pi) \quad \Sigma = \{a/0, b/0, f/1\}$$

$$T_\Sigma = \{a, f(a), f(f(a)), \dots\}^0$$

$$\{b, f(b), f(f(b)), \dots\} = \{f^n(a) \mid n \in \mathbb{N}\} \cup \{f^n(b) \mid n \in \mathbb{N}\}$$

$$A = (T_\Sigma, \{a_A, b_A, f_A : T_\Sigma \rightarrow T_\Sigma\}, \dots)$$

$$a_A = a \in T_\Sigma$$

$$b_A = b \in T_\Sigma$$

$$f_A(t) = f(t) \quad \text{also:} \quad f_A(f^n(a)) = f^{n+1}(a)$$

$$f_A(f^n(b)) = f^{n+1}(b)$$

Beispiel 4

$$\Sigma = (\Sigma, \pi) \quad \Sigma = \{a/0, f/1, g/2\}$$

$$T_\Sigma = \{a, f(a), f^2(a), \dots\}^0 \cup \{g(a, a), g(a, f(a)),$$

$$g(f(a), f(a)), g(a, f^2(a)), \dots\}^0 \cup$$

$$\{f(g(a, a)), f(g(a, f(a))), \dots\}^0.$$

$$A = (T_\Sigma, \{a_A, f_A, g_A : T_\Sigma \times T_\Sigma \rightarrow T_\Sigma\}, \dots)$$

$$a_A = a \in T_\Sigma$$

$$f_A(t) = f(t)$$

$$g_A(t_1, t_2) = g(t_1, t_2)$$

$$\text{z.B.: } g_A(a, f(g(a, a))) \\ = g(a, f(g(a, a))).$$